# Common Time Variation of Parameters in Reduced-Form Macroeconomic Models 

## SUPPLEMENTARY MATERIAL

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#### Abstract

This document contains supplementary material for the paper entitled "Common Time Variation of Parameters in Reduced-Form Macroeconomic Models". It contains: (i) additional simulation results, (ii) additional empirical results, and (iii) data appendix.


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## 1 Additional simulation results

In this section I present standard graphical analysis of the factor structure, scree and trace tests, from the Monte Carlo experiment. The simulation models are summarized as follows:

- Model 1: Univariate Factor-TVP Regression

$$
\begin{align*}
y_{t} & =x_{t}^{\prime} \beta_{t}+w_{t}  \tag{1}\\
\beta_{t} & =\lambda f_{t}+\sigma_{\beta} e_{t}  \tag{2}\\
f_{t+1} & =\rho f_{t}+v_{t+1} \tag{3}
\end{align*}
$$

where $y_{t}$ is a scalar, $x_{t}$ is $(K \times 1)$ and $f_{t}$ contains $q$ elements. The error terms are all drawn independently from a standardized Normal distribution. $\sigma_{\beta}$ is the variance of $e_{t}$, and in particular when it is equal to 0 , we have a case where the time-varying parameters are exact linear combinations of underlying common shocks. Note that $x_{t}$ includes the constant. The parameters are set as follows: $T=300, N=1, K=6, q=1, \sigma_{\beta}=0.4, \rho=0.95$ and $Q=0.1$.

- Model 2: Multivariate Factor-TVP Regression

$$
y_{t}=c_{t}+b_{t} x_{t}+w_{t}
$$

where $y_{t}$ is $(N \times 1)$ and $x_{t}$ contains $K$ independent variables. Let $X_{t}=I_{N} \otimes\left[1, x_{t}^{\prime}\right]$ and $\beta_{t}=\left[\operatorname{vec}\left(c_{t}\right)^{\prime}, \quad \operatorname{vec}\left(b_{t}\right)^{\prime}\right]^{\prime}$ contains all the $K(N+1)$ time-varying coefficients. Then the Factor-TVP is

$$
\begin{equation*}
y_{t}=X_{t}^{\prime} \beta_{t}+w_{t} \tag{4}
\end{equation*}
$$

with (2)-(3) describing the TVPs dynamics. The parameters are set as follows: $T=600$, $N=4, K=4, q=3, \sigma_{\beta}=0.4, \rho=\operatorname{diag}(0.950 .90 .85)$ and $Q=\operatorname{diag}(0.4)$.

- Model 3: Factor-TVP VAR

I consider only $\operatorname{VAR}(1)$ specification since it is always possible to rewrite the $\operatorname{VAR}(p)$ in its companion form:

$$
y_{t}=c_{t}+b_{t} y_{t-1}+w_{t} .
$$

The Factor-TVP representation is the same as in the previous multivariate case, but the number of elements in $\beta_{t}$ is $N(N+1) .{ }^{1}$ The parameters are set as follows: $T=300, N=3$,

[^1]$$
p=1, q=1, \sigma_{\beta}=0.4, \rho=\operatorname{diag}(0.95) \text { and } Q=\operatorname{diag}(0.1)
$$

The results are presented in Figures 1-3. They suggest that the sorting eigenvalues can detect the presence of the factor structure and even recover the true number of latent factors.

## 2 Additional results from TVP-VAR application

In this section I present additional results from TVP-VAR applications. Figures 4-5 verify if the linearity approximation of the factor structure is plausible for the TVPs estimated recursively without stochastic volatility. Recall that TVPs in estimable models will in general be nonlinear functions of the true latent drifting coefficients (or components). To make it feasible and tractable, I approximate it by a linear factor model. According to graphs, the linear hypothesis seems plausible, but adding a polynomial structure would capture some nonlinearities. Figure 6 plots the marginal contribution of first 4 factors to the variance of each of these OLS estimated TVPs. The coefficients of the interest rate equation are mostly explained by the first factor. The same factor is important for some parameters in two other VAR equations, together with the second and third common component.

Figures 7 - 8 show that linearity assumption, within TVPs estimated by likelihood method without factor structure, is quite realistic especially with respect to the first factor. Figure 9 shows the predominance of the first factor to explain the variability in TVPs.

Figures 10 and 11 present the factorability of TVPs and marginal contribution of factors within two-step rolling OLS procedure on the data set updated to 2013Q4. The Figure 12 present the stability condition for the Factor-TVP VAR estimated on data set updated to 2013Q4.

Figures 13 and 16 show the $R^{2}$ between individual time series of the large macroeconomic panel, grouped by category, and the corresponding factors.

The predictive content of TVP factors is studied in Figures 17 and 20. It shows the p-values for null hypothesis $\beta_{h}=0$ from the predictive regression

$$
\begin{equation*}
\hat{f}_{t}^{i}=\alpha+\rho \hat{f}_{t-1}^{i}+\beta \hat{F}_{t-1}^{i}+u_{t} \tag{5}
\end{equation*}
$$

where $i \in(2006,2013)$.

Figure 1: Scree and trace tests from simulations with Model 1





This Figure presents sorted eigenvalues of the correlation matrix of TVPs (scree test), as well as the proportion of their variance explained by consecutive factors (trace test). TVPs have been estimated by rolling least squares (top panels) or ML without factor structure (bottom panels). The Model 1 corresponds to the univariate regression with drifting coefficients generated from the factor structure (2)-(3).

Figure 2: Scree and trace tests from simulations with Model 2


This Figure presents sorted eigenvalues of the correlation matrix of TVPs (scree test), as well as the proportion of their variance explained by consecutive factors (trace test). These are medians over all simulation replications. TVPs have been estimated by rolling least squares (top panels) or ML without factor structure (bottom panels). The Model 2 corresponds to the multivariate regression with drifting coefficients generated from the factor structure (2)-(3).

Figure 3: Scree and trace tests from simulations with Model 3


This Figure presents sorted eigenvalues of the correlation matrix of TVPs (scree test), as well as the proportion of their variance explained by consecutive factors (trace test). These are medians over all simulation replications. TVPs have been estimated by rolling least squares (top panels) or ML without factor structure (bottom panels). The Model 3 corresponds to the TVP-VAR with drifting coefficients generated from the factor structure (2)-(3).

Figure 4: Scatter plots for factor 1 and VAR model TVPs estimated by rolling OLS


This Figure inspects linear factor structure assumption. TVPs have been estimated by rolling least squares. The first factor is the first principal component. The graphs present scatter plots between each VAR time-varying coefficient and the linear fit with the first factor.

Figure 5: Scatter plots for factor 2 and VAR model TVPs estimated by rolling OLS

$$
\lambda_{\mathrm{i}, 2}=0.070379 \quad \lambda_{\mathrm{i}, 2}=0.90182
$$

$$
\lambda_{\mathrm{i}, 2}=-0.10369
$$

$$
\begin{gathered}
-2 \quad \sum_{\lambda_{i, 2}=-0.27326}^{0} \\
0
\end{gathered}
$$

$$
\underbrace{\infty}_{-2} \frac{2}{0}
$$













This Figure inspects linear factor structure assumption. TVPs have been estimated by rolling least squares. The second factor is the second principal component. The graphs present scatter plots between each VAR time-varying coefficient and the linear fit with the second factor.

Figure 6: Marginal contributions of factors to total $R_{2}$ on TVPs estimated by rolling OLS


This Figure decompose the contribution of first 4 principal components to the variance of each TVP estimated using rolling least squares. The elements 1-7 represent coefficients from inflation equation, $\left[b_{0,1}, b_{1,11}, b_{1,12}, \ldots b_{2,13}\right], 8-14$ those from unemployment rate equation and 15-21 for interest rate.

Figure 7: Scatter plots for factor 1 and VAR model TVPs estimated by two-step likelihood method


This Figure inspects linear factor structure assumption. TVPs are those from Primiceri (2005). The first factor is estimated by MLE. The graphs present scatter plots between each VAR time-varying coefficient and the linear fit with the first factor.

Figure 8: Scatter plots for factor 2 and VAR model TVPs estimated by two-step likelihood method


This Figure inspects linear factor structure assumption. TVPs are those from Primiceri (2005). The second factor is estimated by MLE. The graphs present scatter plots between each VAR time-varying coefficient and the linear fit with the second factor.

Figure 9: Marginal contribution to total $R^{2}$ of TVPs of VAR estimated by two-step likelihood method


This Figure decompose the contribution of first 5 MLE factors to the variance of each TVP estimated as in Primiceri (2005) without imposing factor structure. The elements 1-7 represent coefficients from inflation equation, $\left[b_{0,1}, b_{1,11}, b_{1,12}, \ldots b_{2,13}\right]$, 8-14 those from unemployment rate equation and 15-21 for interest rate.

Figure 10: Scree and trace tests for VAR model TVPs estimated by recursive OLS


Cumulative product of eigenvalues


Cumulative ratio of eigenvalues



This Figure presents sorted eigenvalues of the correlation matrix of TVPs (scree test), their cumulated product and ratio, as well as the proportion of TVP variances explained by consecutive factors (trace test). TVPs have been estimated by rolling least squares on data set updated to 2013Q4.

Figure 11: Marginal contributions to total $R^{2}$ on VAR model TVPs estimated by recursive OLS with post-crisis data


This Figure decompose the contribution of first 4 principal components to the variance of each TVP estimated using rolling least squares on the updated data set including the Great Recession period. The elements 1-7 represent coefficients from inflation equation, $\left[b_{0,1}, b_{1,11}, b_{1,12}, \ldots b_{2,13}\right], 8-14$ those from unemployment rate equation and 15-21 for interest rate.

Figure 12: Stability of Factor-TVP VAR over time with post-crisis data


This Figure shows the largest eigenvalue of the companion matrix of the VAR coefficients, at each point of time. The TVPs are calculated as the common component after all the Factor-TVP equations have been estimated simultaneously by maximum likelihood and on the data set updated to 2013Q4. The stability condition is violated if larger than 1.

Figure 13: $R^{2}$ Between Factors and Individual Time Series, Grouped by Category


This Figure shows marginal $R^{2}$ of factors 1-5 estimated from large the macroeconomic data set on each 141 series grouped by category. Data span is 1959-2006. The meaning of each acronym is the following. OUT: Real output and income, CONS: Real consumption; INVST: Real investment, EMP: Employment and hours; INV: Inventories; MON: Money and credit quantity aggregates; PRI: Price indexes; AHE: Average hourly earnings and salaries; GOV: Government spending and revenues.

Figure 14: $R^{2}$ Between Factors and Individual Time Series, Grouped by Category


Figure 15: $R^{2}$ Between Factors and Individual Time Series, Grouped by Category


This Figure shows marginal $R^{2}$ of factors 1-5 estimated from large the macroeconomic data set on each 141 series grouped by category. Data span is 1959-2013. The meaning of each acronym is the following. OUT: Real output and income, CONS: Real consumption; INVST: Real investment, EMP: Employment and hours; INV: Inventories; MON: Money and credit quantity aggregates; PRI: Price indexes; AHE: Average hourly earnings and salaries; GOV: Government spending and revenues.

Figure 16: $R^{2}$ Between Factors and Individual Time Series, Grouped by Category


Figure 17: Predictive power of TVP factors from data set 1959-2006


This Figure shows the predictive power of two TVP factors for each of 141 series grouped by category. It plots the p-values for null hypothesis $\beta_{h}=0$ from the predictive regression (5). The black horizontal line fix the level of $5 \%$. The meaning of each acronym is the following. OUT: Real output and income, CONS: Real consumption; INVST: Real investment, EMP: Employment and hours; INV: Inventories; MON: Money and credit quantity aggregates; PRI: Price indexes; AHE: Average hourly earnings and salaries; GOV: Government spending and revenues.

Figure 18: Predictive power of TVP factors from data set 1959-2006


This Figure shows the predictive power of two TVP factors for each of 141 series grouped by category. It plots the p-values for null hypothesis $\beta_{h}=0$ from the predictive regression (5). The black horizontal line fix the level of $5 \%$. The meaning of each acronym is the following. OUT: Real output and income, CONS: Real consumption; INVST: Real investment, EMP: Employment and hours; INV: Inventories; MON: Money and credit quantity aggregates; PRI: Price indexes; AHE: Average hourly earnings and salaries; GOV: Government spending and revenues.

Figure 19: Predictive power of TVP factors from data set 1959-2013


This Figure shows the predictive power of two TVP factors for each of 141 series grouped by category. It plots the p-values for null hypothesis $\beta_{h}=0$ from the predictive regression (5). The black horizontal line fix the level of $5 \%$. The meaning of each acronym is the following. OUT: Real output and income, CONS: Real consumption; INVST: Real investment, EMP: Employment and hours; INV: Inventories; MON: Money and credit quantity aggregates; PRI: Price indexes; AHE: Average hourly earnings and salaries; GOV: Government spending and revenues.

Figure 20: Predictive power of TVP factors from data set 1959-2013


This Figure shows the predictive power of two TVP factors for each of 141 series grouped by category. It plots the p-values for null hypothesis $\beta_{h}=0$ from the predictive regression (5). The black horizontal line fix the level of $5 \%$. The meaning of each acronym is the following. OUT: Real output and income, CONS: Real consumption; INVST: Real investment, EMP: Employment and hours; INV: Inventories; MON: Money and credit quantity aggregates; PRI: Price indexes; AHE: Average hourly earnings and salaries; GOV: Government spending and revenues.

## 3 Data appendix

The 141 series in the large macroeconomic panel are detailed in the following table. All series have been transform to achieve stationarity. The transformation codes are: 1 no transformation; 2 first
difference; 4 logarithm; 5 first difference of logarithm.

| No. | Series Code |
| :--- | :--- |
| 1 | USAPROINDQISMEI |
| 2 | GDPC1 |
| 3 | PIECTR |
| 4 | INDPRO |
| 5 | IPBUSEQ |
| 6 | IPCONGD |
| 7 | IPDCONGD |
| 8 | IPDMAT |
| 9 | IPFINAL |
| 10 | IPFPNSS |
| 11 | IPFUELS |
| 12 | IPMANSICS |
| 13 | IPMAT |
| 14 | IPNCONGD |
| 15 | IPNMAT |
| 16 | NAPMPI |
| 17 | CUMFNS |
| 18 | USAPROINDMISMEI |
| 19 | DGDSRC1Q027SBEA |
| 20 | PCECC96 |
| 21 | DPCERA3Q086SBEA |
| 22 | DDURRA3Q086SBEA |
| 23 | DNDGRA3Q086SBEA |
| 24 | DSERRA3Q086SBEA |
| 25 | W170RC1Q027SBEA |
| 26 | GPDIC1 |
| 27 | GPDIC96 |
| 28 | A349RA3Q086SBEA |
| 29 | A756RA3Q086SBEA |
| 30 | A771RA3Q086SBEA |
| 31 | B006RA3Q086SBEA |
| 32 | B007RA3Q086SBEA |
| 33 | B008RA3Q086SBEA |
| 34 | B009RA3Q086SBEA |
| 35 | B011RA3Q086SBEA |
| 36 | B012RA3Q086SBEA |
| 37 | B013RA3Q086SBEA |
| 38 | B139RA3Q086SBEA |
| 39 | B292RA3Q086SBEA |
| 40 | B679RA3Q086SBEA |
| 41 | B680RA3Q086SBEA |
| 42 | B681RA3Q086SBEA |
| 43 | B862RA3Q086SBEA |
| 44 | B863RA3Q086SBEA |
| 45 | B937RA3Q086SBEA |
| 46 | B943RA3Q086SBEA |
| 47 | B944RA3Q086SBEA |
| 48 | C307RA3Q086SBEA |
| 49 | E318RA3Q086SBEA |
| 50 | W001RA3Q086SBEA |
| 51 | W003RA3Q086SBEA |
| 52 | W004RA3Q086SBEA |
| 53 | W040RA3Q086SBEA |
| 54 | PRS85006013 |
| 55 | PRS88003013 |
| 56 | CES1021000001 |
| 57 | CLF16OV |
| 58 | DMANEMP |
| 59 | MANEMP |
| 60 | NAPMEI |
| 61 | NDMANEMP |
| 63 | PAYEMS |
|  | SRVPRD |


| T-Code | Series Description |
| :---: | :---: |
| 5 | Production of Total Industry in United States |
| 5 | Real Gross Domestic Product |
| 5 | Real personal income excluding current transfer receipts |
| 5 | Industrial Production Index |
| 5 | Industrial Production: Business Equipment |
| 5 | Industrial Production: Consumer Goods |
| 5 | Industrial Production: Durable Consumer Goods |
| 5 | Industrial Production: Durable Materials |
| 5 | Industrial Production: Final Products (Market Group) |
| 5 | Industrial Production: Final Products and Nonindustrial Supplies |
| 5 | Industrial Production: Fuels |
| 5 | Industrial Production: Manufacturing (SIC) |
| 5 | Industrial Production: Materials |
| 5 | Industrial Production: Nondurable Consumer Goods |
| 5 | Industrial Production: nondurable Materials |
| 1 | ISM Manufacturing: Production Index |
| 1 | Capacity Utilization: Manufacturing (SIC) |
| 5 | Production of Total Industry in United States |
| 5 | Personal consumption expenditures: Goods |
| 5 | Real Personal Consumption Expenditures |
| 5 | Real personal consumption expenditures (chain-type quantity index) |
| 5 | Real personal consumption expenditures: Durable goods (chain-typequantity index) |
| 5 | Real personal consumption expenditures: Nondurable goods (chain-typequantity index) |
| 5 | Real personal consumption expenditures: Services (chain-type quantityindex) |
| 5 | Gross domestic investment |
| 5 | Real Gross Private Domestic Investment |
| 5 | Real Gross Private Domestic Investment, 3 decimal |
| 5 | Real private fixed investment in structures (chain-type quantityindex) |
| 5 | Real private fixed investment in new structures: Residentialstructures (chain-type quantity index) |
| 5 | Real private fixed investment in new structures: Nonresidentialstructures (chain-type quantity index) |
| 5 | Real gross private domestic investment (chain-type quantity index) |
| 5 | Real private fixed investment (chain-type quantity index) |
| 5 | Real private fixed investment: Nonresidential (chain-type quantityindex) |
| 5 | Real private fixed investment: Nonresidential: Structures (chain-typequantity index) |
| 5 | Real private fixed investment: Residential (chain-type quantity index) |
| 5 | Real private fixed investment: Residential: Structures (chain-typequantity index) |
| 5 | Real private fixed investment: Residential: Equipment (chain-typequantity index) |
| 5 | Real auto output: Private fixed investment: New autos (chain-typequantity index) |
| 5 | Real private fixed investment: Residential: Structures: Permanentsite: Multifamily (chain-type quantity index) |
| 5 | Real private fixed investment, chained quantity index: Private fixedinvestment in information processing equipment and |
| 5 | Real private fixed investment, chained quantity index: Nonresidential:Equipment: Industrial equipment |
| 5 | Real private fixed investment, chained quantity index: Nonresidential:Equipment: Transportation equipment |
| 5 | Real private fixed investment, chained quantity index: Nonresidential:Equipment: Other equipment |
| 5 | Real private fixed investment: Residential: Other structures(chain-type quantity index) |
| 5 | Real private fixed investment, chained quantity index: Nonresidential:Equipment: Information processing equipment: O |
| 5 | Real private fixed investment: Residential: Structures: Permanent site(chain-type quantity index) |
| 5 | Real private fixed investment: Residential: Structures: Permanentsite: Single family (chain-type quantity index) |
| 5 | Real private fixed investment: Nonresidential: Structures: Manufacturing (chain-type quantity index) |
| 5 | Real private fixed investment: Nonresidential: Structures: Miningexploration, shafts, and wells (chain-type quantity ind |
| 5 | Real private fixed investment: Nonresidential: Structures: Commercialand health care (chain-type quantity index) |
| 5 | Real private fixed investment: Nonresidential: Structures: Power andcommunication (chain-type quantity index) |
| 5 | Real private fixed investment: Nonresidential: Other structures(chain-type quantity index) |
| 5 | Real private fixed investment in new structures (chain-type quantityindex) |
| 5 | Nonfarm Business Sector: Employment |
| 5 | Nonfinancial Corporations Sector: Employment |
| 5 | All Employees: Mining and Logging: Mining |
| 5 | Civilian Labor Force |
| 5 | All Employees: Durable goods |
| 5 | All Employees: Manufacturing |
| 1 | ISM Manufacturing: Employment Index |
| 5 | All Employees: Nondurable goods |
| 5 | All Employees: Total nonfarm |
| 5 | All Employees: Service-Providing Industries |


| 64 | UEMP15OV | 5 |
| :---: | :---: | :---: |
| 65 | UEMP15T26 | 5 |
| 66 | UEMP27OV | 5 |
| 67 | UEMP5TO14 | 5 |
| 68 | UEMPLT5 | 5 |
| 69 | UEMPMEAN | 5 |
| 70 | UNRATE | 1 |
| 71 | USFIRE | 5 |
| 72 | USGOOD | 5 |
| 73 | USGOVT | 5 |
| 74 | USTPU | 5 |
| 75 | USTRADE | 5 |
| 76 | USWTRADE | 5 |
| 77 | CE16OV | 5 |
| 78 | USCONS | 5 |
| 79 | HOABS | 5 |
| 80 | HOANBS | 5 |
| 81 | PRS84006023 | 1 |
| 82 | PRS85006023 | 1 |
| 83 | AWHMAN | 1 |
| 84 | AWOTMAN | 1 |
| 85 | A371RX1Q020SBEA | 5 |
| 86 | A373RX1Q020SBEA | 5 |
| 87 | B372RX1Q020SBEA | 5 |
| 88 | NAPMII | 1 |
| 89 | NAPMNOI | 1 |
| 90 | NAPMSDI | 1 |
| 91 | NAPM | 1 |
| 92 | SP500 | 5 |
| 93 | AAA | 1 |
| 94 | BAA | 1 |
| 95 | FEDFUNDS | 1 |
| 96 | GS1 | 1 |
| 97 | GS10 | 1 |
| 98 | GS5 | 1 |
| 99 | TB3MS | 1 |
| 100 | AAA-S | 1 |
| 101 | BAA-S | 1 |
| 102 | GS1-S | 1 |
| 103 | GS10-S | 1 |
| 104 | GS5-S | 1 |
| 105 | TB3MS-S | 1 |
| 106 | TB6MS-S | 1 |
| 107 | AMBSL | 5 |
| 108 | BUSLOANS | 5 |
| 109 | NONREVSL | 5 |
| 110 | REALLN | 5 |
| 111 | DTCOLNVHFNM | 5 |
| 112 | DTCTHFNM | 5 |
| 113 | INVEST | 5 |
| 114 | CPIAUCSL | 5 |
| 115 | CPIAPPSL | 5 |
| 116 | CPITRNSL | 5 |
| 117 | CPIMEDSL | 5 |
| 118 | CUSR0000SAC | 5 |
| 119 | CUUR0000SAD | 5 |
| 120 | CUSR0000SAS | 5 |
| 121 | CPIULFSL | 5 |
| 122 | CUUR0000SA0L2 | 5 |
| 123 | CUSR0000SA0L5 | 5 |
| 124 | PPICMM | 5 |
| 125 | PPICRM | 5 |
| 126 | PPIFCG | 5 |
| 127 | PPIFGS | 5 |
| 128 | PPIIDC | 5 |
| 129 | NAPMPRI | 1 |
| 130 | A132RC1Q027SBEA | 5 |
| 131 | B202RC1Q027SBEA | 5 |
| 132 | COMPNFB | 5 |
| 133 | HCOMPBS | 5 |
| 134 | W209RC1Q027SBEA | 5 |
| 135 | COMPRNFB | 5 |
| 136 | RCPHBS | 5 |
| 137 | CES0600000008 | 5 |



| 138 | CES2000000008 | 5 |
| :--- | :--- | :--- |
| 139 | CES3000000008 | 5 |
| 140 | GCEC96 | 5 |
| 141 | W066RC1Q027SBEA | 5 |

Average Hourly Earnings of Production and Nonsupervisory Employees:Construction Average Hourly Earnings of Production and Nonsupervisory Employees:Manufacturing Real Government Consumption Expenditures \& Gross Investment
Government total receipts


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[^1]:    ${ }^{1}$ The simulation of TVP-VAR model is tricky. To avoid explosive roots, for each $t$, I decompose $b_{t}$ using singular value decomposition and check if the eigenvalues of $b_{t}$ are inside the unit circle. If not, I scale them such that they are less than one and reproduce the corresponding coefficient matrix.

